

For use in exams from the June 2017 Series onwards

DATA - FUNDAMENTAL CONSTANTS AND VALUES

Quantity	Symbol	Value	Units
speed of light in vacuo	c	3.00×10^8	m s^{-1}
permeability of free space	μ_0	$4\pi \times 10^{-7}$	H m^{-1}
permittivity of free space	ϵ_0	8.85×10^{-12}	F m^{-1}
magnitude of the charge of electron	e	1.60×10^{-19}	C
the Planck constant	h	6.63×10^{-34}	J s
gravitational constant	G	6.67×10^{-11}	$\text{N m}^2 \text{kg}^{-2}$
the Avogadro constant	N_A	6.02×10^{23}	mol^{-1}
molar gas constant	R	8.31	$\text{J K}^{-1} \text{mol}^{-1}$
the Boltzmann constant	k	1.38×10^{-23}	J K^{-1}
the Stefan constant	σ	5.67×10^{-8}	$\text{W m}^{-2} \text{K}^{-4}$
the Wien constant	α	2.90×10^{-3}	m K
electron rest mass (equivalent to 5.5×10^{-4} u)	m_e	9.11×10^{-31}	kg
magnitude of electron charge/mass ratio	$\frac{e}{m_e}$	1.76×10^{11}	C kg^{-1}
proton rest mass (equivalent to 1.00728 u)	m_p	$1.67(3) \times 10^{-27}$	kg
proton charge/mass ratio	$\frac{e}{m_p}$	9.58×10^7	C kg^{-1}
neutron rest mass (equivalent to 1.00867 u)	m_n	$1.67(5) \times 10^{-27}$	kg
gravitational field strength	g	9.81	N kg^{-1}
acceleration due to gravity	g	9.81	m s^{-2}
atomic mass unit (1u is equivalent to 931.5 MeV)	u	1.661×10^{-27}	kg

ALGEBRAIC EQUATION

quadratic equation $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

ASTRONOMICAL DATA

Body	Mass/kg	Mean radius/m
Sun	1.99×10^{30}	6.96×10^8
Earth	5.97×10^{24}	6.37×10^6

GEOMETRICAL EQUATIONS

arc length $= r\theta$
 circumference of circle $= 2\pi r$
 area of circle $= \pi r^2$
 curved surface area of cylinder $= 2\pi rh$
 surface area of sphere $= 4\pi r^2$
 volume of sphere $= \frac{4}{3}\pi r^3$

Particle Physics

Class	Name	Symbol	Rest energy/MeV
photon	photon	γ	0
lepton	neutrino	ν_e	0
		ν_μ	0
	electron	$e^\pm$	0.510999
	muon	$\mu^\pm$	105.659
mesons	π meson	$\pi^\pm$	139.576
		π^0	134.972
	K meson	$K^\pm$	493.821
		K^0	497.762
baryons	proton	p	938.257
	neutron	n	939.551

Properties of quarks

antiquarks have opposite signs

Type	Charge	Baryon number	Strangeness
u	$+\frac{2}{3}e$	$+\frac{1}{3}$	0
d	$-\frac{1}{3}e$	$+\frac{1}{3}$	0
s	$-\frac{1}{3}e$	$+\frac{1}{3}$	-1

Properties of Leptons

	Lepton number
Particles: $e^-, \nu_e; \mu^-, \nu_\mu$	+1
Antiparticles: $e^+, \bar{\nu}_e, \mu^+, \bar{\nu}_\mu$	-1

Photons and energy levels

photon energy $E = hf = \frac{hc}{\lambda}$
photoelectricity $hf = \phi + E_{k(\max)}$
energy levels $hf = E_1 - E_2$
de Broglie wavelength $\lambda = \frac{h}{p} = \frac{h}{mv}$

Waves

wave speed $c = f\lambda$ *period* $f = \frac{1}{T}$
first harmonic $f = \frac{1}{2l} \sqrt{\frac{T}{\mu}}$
fringe spacing $w = \frac{\lambda D}{s}$ *diffraction grating* $d \sin \theta = n\lambda$
refractive index of a substance s, $n = \frac{c}{c_s}$
for two different substances of refractive indices n_1 and n_2 ,
law of refraction $n_1 \sin \theta_1 = n_2 \sin \theta_2$
critical angle $\sin \theta_c = \frac{n_2}{n_1}$ for $n_1 > n_2$

Mechanics

moments *moment* $= Fd$
velocity and acceleration $v = \frac{\Delta s}{\Delta t}$ $a = \frac{\Delta v}{\Delta t}$
equations of motion $v = u + at$ $s = \left(\frac{u+v}{2}\right)t$
 $v^2 = u^2 + 2as$ $s = ut + \frac{at^2}{2}$
force $F = ma$
force $F = \frac{\Delta(mv)}{\Delta t}$
impulse $F \Delta t = \Delta(mv)$
work, energy and power $W = F s \cos \theta$
 $E_k = \frac{1}{2} m v^2$ $\Delta E_p = mg \Delta h$
 $P = \frac{\Delta W}{\Delta t}, P = Fv$
efficiency $= \frac{\text{useful output power}}{\text{input power}}$

Materials

density $\rho = \frac{m}{V}$ *Hooke's law* $F = k \Delta L$
Young modulus $= \frac{\text{tensile stress}}{\text{tensile strain}}$ *tensile stress* $= \frac{F}{A}$
tensile strain $= \frac{\Delta L}{L}$
energy stored $E = \frac{1}{2} F \Delta L$

Electricity

$$\text{current and pd} \quad I = \frac{\Delta Q}{\Delta t} \quad V = \frac{W}{Q} \quad R = \frac{V}{I}$$

$$\text{resistivity} \quad \rho = \frac{RA}{L}$$

$$\text{resistors in series} \quad R_T = R_1 + R_2 + R_3 + \dots$$

$$\text{resistors in parallel} \quad \frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots$$

$$\text{power} \quad P = VI = I^2R = \frac{V^2}{R}$$

$$\text{emf} \quad \varepsilon = \frac{E}{Q} \quad \varepsilon = I(R + r)$$

Circular motion

$$\text{magnitude of angular speed} \quad \omega = \frac{v}{r}$$

$$\omega = 2\pi f$$

$$\text{centripetal acceleration} \quad a = \frac{v^2}{r} = \omega^2 r$$

$$\text{centripetal force} \quad F = \frac{mv^2}{r} = m\omega^2 r$$

Simple harmonic motion

$$\text{acceleration} \quad a = -\omega^2 x$$

$$\text{displacement} \quad x = A \cos(\omega t)$$

$$\text{speed} \quad v = \pm \omega \sqrt{(A^2 - x^2)}$$

$$\text{maximum speed} \quad v_{\max} = \omega A$$

$$\text{maximum acceleration} \quad a_{\max} = \omega^2 A$$

$$\text{for a mass-spring system} \quad T = 2\pi \sqrt{\frac{m}{k}}$$

$$\text{for a simple pendulum} \quad T = 2\pi \sqrt{\frac{l}{g}}$$

Thermal physics

$$\text{energy to change temperature} \quad Q = mc\Delta\theta$$

$$\text{energy to change state} \quad Q = ml$$

$$\text{gas law} \quad pV = nRT$$

$$pV = NkT$$

$$\text{kinetic theory model} \quad pV = \frac{1}{3}Nm(c_{\text{rms}})^2$$

$$\text{kinetic energy of gas molecule} \quad \frac{1}{2}m(c_{\text{rms}})^2 = \frac{3}{2}kT = \frac{3RT}{2N_A}$$

Gravitational fields

$$\text{force between two masses} \quad F = \frac{Gm_1m_2}{r^2}$$

$$\text{gravitational field strength} \quad g = \frac{F}{m}$$

$$\text{magnitude of gravitational field strength in a radial field} \quad g = \frac{GM}{r^2}$$

$$\text{work done} \quad \Delta W = m\Delta V$$

$$\text{gravitational potential} \quad V = -\frac{GM}{r}$$

$$g = -\frac{\Delta V}{\Delta r}$$

Electric fields and capacitors

$$\text{force between two point charges} \quad F = \frac{1}{4\pi\epsilon_0} \frac{Q_1Q_2}{r^2}$$

$$\text{force on a charge} \quad F = EQ$$

$$\text{field strength for a uniform field} \quad E = \frac{V}{d}$$

$$\text{work done} \quad \Delta W = Q\Delta V$$

$$\text{field strength for a radial field} \quad E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r^2}$$

$$\text{electric potential} \quad V = \frac{1}{4\pi\epsilon_0} \frac{Q}{r}$$

$$\text{field strength} \quad E = \frac{\Delta V}{\Delta r}$$

$$\text{capacitance} \quad C = \frac{Q}{V}$$

$$C = \frac{A\epsilon_0\epsilon_r}{d}$$

$$\text{capacitor energy stored} \quad E = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2} \frac{Q^2}{C}$$

$$\text{capacitor charging} \quad Q = Q_0(1 - e^{-\frac{t}{RC}})$$

$$\text{decay of charge} \quad Q = Q_0 e^{-\frac{t}{RC}}$$

$$\text{time constant} \quad RC$$

Magnetic fields

<i>force on a current</i>	$F = BIl$
<i>force on a moving charge</i>	$F = BQv$
<i>magnetic flux</i>	$\Phi = BA$
<i>magnetic flux linkage</i>	$N\Phi = BAN \cos \theta$
<i>magnitude of induced emf</i>	$\varepsilon = N \frac{\Delta\Phi}{\Delta t}$
	$N\Phi = BAN \cos \theta$
<i>emf induced in a rotating coil</i>	$\varepsilon = BAN\omega \sin \omega t$
<i>alternating current</i>	$I_{\text{rms}} = \frac{I_0}{\sqrt{2}} \quad V_{\text{rms}} = \frac{V_0}{\sqrt{2}}$
<i>transformer equations</i>	$\frac{N_s}{N_p} = \frac{V_s}{V_p}$
	$\text{efficiency} = \frac{I_s V_s}{I_p V_p}$

Nuclear physics

<i>inverse square law for γ radiation</i>	$I = \frac{k}{x^2}$
<i>radioactive decay</i>	$\frac{\Delta N}{\Delta t} = -\lambda N, N = N_0 e^{-\lambda t}$
<i>activity</i>	$A = \lambda N$
<i>half-life</i>	$T_{1/2} = \frac{\ln 2}{\lambda}$
<i>nuclear radius</i>	$R = R_0 A^{1/3}$
<i>energy-mass equation</i>	$E = mc^2$

OPTIONS

Astrophysics

1 astronomical unit	$= 1.50 \times 10^{11} \text{ m}$
1 light year	$= 9.46 \times 10^{15} \text{ m}$
1 parsec	$= 2.06 \times 10^5 \text{ AU} = 3.08 \times 10^{16} \text{ m}$
	$= 3.26 \text{ ly}$

Hubble constant, $H = 65 \text{ km s}^{-1} \text{ Mpc}^{-1}$

$$M = \frac{\text{angle subtended by image at eye}}{\text{angle subtended by object at unaided eye}}$$

<i>telescope in normal adjustment</i>	$M = \frac{f_o}{f_e}$
<i>Rayleigh criterion</i>	$\theta \approx \frac{\lambda}{D}$
<i>magnitude equation</i>	$m - M = 5 \log \frac{d}{10}$
<i>Wien's law</i>	$\lambda_{\text{max}} T = 2.9 \times 10^{-3} \text{ m K}$
<i>Stefan's law</i>	$P = \sigma AT^4$
<i>Schwarzschild radius</i>	$R_s \approx \frac{2GM}{c^2}$
<i>Doppler shift for $v \ll c$</i>	$\frac{\Delta f}{f} = -\frac{\Delta \lambda}{\lambda} = \frac{v}{c}$
<i>red shift</i>	$z = -\frac{v}{c}$
<i>Hubble's law</i>	$v = Hd$

Medical physics

<i>lens equations</i>	$P = \frac{1}{f}$
	$m = \frac{v}{u}$
	$\frac{1}{f} = \frac{1}{u} + \frac{1}{v}$
<i>threshold of hearing</i>	$I_0 = 1.0 \times 10^{-12} \text{ W m}^{-2}$
<i>intensity level</i>	$\text{intensity level} = 10 \log \frac{I}{I_0}$
<i>absorption</i>	$I = I_0 e^{-\mu x}$
	$\mu_m = \frac{\mu}{\rho}$
<i>ultrasound imaging</i>	$Z = p c$
	$\frac{I_r}{I_i} = \left(\frac{Z_2 - Z_1}{Z_2 + Z_1} \right)^2$
<i>half-lives</i>	$\frac{1}{T_E} = \frac{1}{T_B} + \frac{1}{T_P}$

Engineering physics

<i>moment of inertia</i>	$I = \Sigma mr^2$
<i>angular kinetic energy</i>	$E_k = \frac{1}{2} I \omega^2$
<i>equations of angular motion</i>	$\omega_2 = \omega_1 + \alpha t$ $\omega_2^2 = \omega_1^2 + 2\alpha\theta$ $\theta = \omega_1 t + \frac{\alpha t^2}{2}$ $\theta = \frac{(\omega_1 + \omega_2) t}{2}$
<i>torque</i>	$T = I \alpha$ $T = F r$
<i>angular momentum</i>	<i>angular momentum</i> = $I \omega$
<i>angular impulse</i>	$T \Delta t = \Delta(I \omega)$
<i>work done</i>	$W = T \theta$
<i>power</i>	$P = T \omega$
<i>thermodynamics</i>	$Q = \Delta U + W$ $W = p \Delta V$
<i>adiabatic change</i>	$p V^\gamma = \text{constant}$
<i>isothermal change</i>	$p V = \text{constant}$
<i>heat engines</i>	
	$\text{efficiency} = \frac{W}{Q_H} = \frac{Q_H - Q_C}{Q_H}$
<i>maximum theoretical efficiency</i>	$\frac{T_H - T_C}{T_H}$
<i>work done per cycle</i>	= <i>area of loop</i>
<i>input power</i>	= <i>calorific value</i> $\times$ <i>fuel flow rate</i>
<i>indicated power</i>	= (<i>area of p – V loop</i>) $\times$ (<i>number of cycles per second</i>) $\times$ (<i>number of cylinders</i>)
<i>output or brake power</i>	$P = T \omega$
<i>friction power</i>	= <i>indicated power</i> – <i>brake power</i>
<i>heat pumps and refrigerators</i>	
<i>refrigerator: COP_{ref}</i>	$= \frac{Q_C}{W} = \frac{Q_C}{Q_H - Q_C}$
<i>heat pump: COP_{hp}</i>	$= \frac{Q_H}{W} = \frac{Q_H}{Q_H - Q_C}$

Turning points in physics

<i>electrons in fields</i>	$F = \frac{eV}{d}$ $F = Bev$ $r = \frac{mv}{Be}$ $\frac{1}{2} mv^2 = eV$
<i>Millikan's experiment</i>	$\frac{QV}{d} = mg$ $F = 6\pi\eta r v$
<i>Maxwell's formula</i>	$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$ $\lambda = \frac{h}{p} = \frac{h}{\sqrt{2meV}}$
<i>special relativity</i>	$t = \frac{t_0}{\sqrt{1 - \frac{v^2}{c^2}}}$ $l = l_0 \sqrt{1 - \frac{v^2}{c^2}}$ $E = mc^2 = \frac{m_0 c^2}{\sqrt{1 - \frac{v^2}{c^2}}}$

Electronics

<i>resonant frequency</i>	$f_0 = \frac{1}{2\pi \sqrt{LC}}$
<i>Q-factor</i>	$Q = \frac{f_0}{f_B}$
<i>operational amplifiers: open loop</i>	$V_{\text{out}} = A_{\text{OL}}(V_+ - V_-)$
<i>inverting amplifier</i>	$\frac{V_{\text{out}}}{V_{\text{in}}} = -\frac{R_f}{R_{\text{in}}}$
<i>non-inverting amplifier</i>	$\frac{V_{\text{out}}}{V_{\text{in}}} = 1 + \frac{R_f}{R_1}$
<i>summing amplifier</i>	$V_{\text{out}} = -R_f \left(\frac{V_1}{R_1} + \frac{V_2}{R_2} + \frac{V_3}{R_3} + \dots \right)$
<i>difference amplifier</i>	$V_{\text{out}} = (V_+ - V_-) \frac{R_f}{R_1}$
<i>Bandwidth requirement:</i>	
<i>for AM</i>	<i>bandwidth</i> = $2f_M$
<i>for FM</i>	<i>bandwidth</i> = $2(\Delta f + f_M)$

