



**FM1 (Year 1) – Coefficient of Restitution With Single Collision Exam Questions (Edexcel)**

**Q1.**

A particle of mass  $m$  kg lies on a smooth horizontal surface. Initially the particle is at rest at a point  $O$  midway between a pair of fixed parallel vertical walls. The walls are 2 m apart. At time  $t = 0$  the particle is projected from  $O$  with speed  $u$  m s<sup>-1</sup> in a direction perpendicular to the walls. The coefficient of restitution between the particle and each wall is  $\frac{2}{3}$ . The magnitude of the impulse on the particle due to the first impact with a wall is  $\lambda mu$  N s.

(a) Find the value of  $\lambda$ .

(3)

The particle returns to  $O$ , having bounced off each wall once, at time  $t = 3$  seconds.

(b) Find the value of  $u$ .

(6)

**(Total 9 marks)**

**(Q02 6678/01, June 2014)**

**Q2.**

Two particles  $P$  and  $Q$ , of masses  $2m$  and  $m$  respectively, are on a smooth horizontal table. Particle  $Q$  is at rest and particle  $P$  collides directly with it when moving with speed  $u$ .

After the collision the total kinetic energy of the two particles is  $\frac{3}{4}mu^2$ . Find

(a) the speed of  $Q$  immediately after the collision,

(10)

(b) the coefficient of restitution between the particles.

(3)

**(Total 13 marks)**

**(Q04 6678/01/R, June 2013)**

**Q3.**

A particle  $P$  of mass  $3m$  is moving with speed  $2u$  in a straight line on a smooth horizontal plane. The particle  $P$  collides directly with a particle  $Q$  of mass  $4m$  moving on the plane with speed  $u$  in the opposite direction to  $P$ . The coefficient of restitution between  $P$  and  $Q$  is  $e$ .

(a) Find the speed of  $Q$  immediately after the collision.

(6)

Given that the direction of motion of  $P$  is reversed by the collision,

(b) find the range of possible values of  $e$ .

(5)

**(Total 11 marks)**

**(Q02 6678/01, June 2012)**



**Q4.**

A particle  $P$  of mass  $m$  is moving in a straight line on a smooth horizontal surface with speed  $4u$ . The particle  $P$  collides directly with a particle  $Q$  of mass  $3m$  which is at rest on the surface. The coefficient of restitution between  $P$  and  $Q$  is  $e$ . The direction of motion of  $P$  is reversed by the collision.

Show that  $e > \frac{1}{3}$

(8)

(Total 8 marks)

(Q03 6678/01, June 2011)

**Q5.**

A particle  $A$  of mass  $4m$  is moving with speed  $3u$  in a straight line on a smooth horizontal table. The particle  $A$  collides directly with a particle  $B$  of mass  $3m$  moving with speed  $2u$  in the same direction as  $A$ . The coefficient of restitution between  $A$  and  $B$  is  $e$ . Immediately after the collision the speed of  $B$  is  $4eu$ .

(a) Show that  $e = \frac{3}{4}$

(5)

(b) Find the total kinetic energy lost in the collision.

(4)

(Total 9 marks)

(Q03 6678/01, June 2008)

**Q6.**

Two particles,  $P$ , of mass  $2m$ , and  $Q$ , of mass  $m$ , are moving along the same straight line on a smooth horizontal plane. They are moving in opposite directions towards each other and collide. Immediately before the collision the speed of  $P$  is  $2u$  and the speed of  $Q$  is  $u$ . The coefficient of restitution between the particles is  $e$ , where  $e < 1$ . Find, in terms of  $u$  and  $e$ ,

(i) the speed of  $P$  immediately after the collision,

(ii) the speed of  $Q$  immediately after the collision.

(7)

(Total 7 marks)

(Q02 6678/01, Jan 2010)

**Q7.**

A particle  $P$  of mass  $m$  kg is moving with speed  $6 \text{ m s}^{-1}$  in a straight line on a smooth horizontal floor. The particle strikes a fixed smooth vertical wall at right angles and rebounds. The kinetic energy lost in the impact is  $64 \text{ J}$ . The coefficient of restitution between  $P$  and the wall is  $\frac{1}{3}$ .

(a) Show that  $m = 4$ .

(6)

After rebounding from the wall,  $P$  collides directly with a particle  $Q$  which is moving towards  $P$  with speed  $3 \text{ m s}^{-1}$ . The mass of  $Q$  is  $2 \text{ kg}$  and the coefficient of restitution between  $P$  and  $Q$  is  $\frac{1}{3}$ .

(b) Show that there will be a second collision between  $P$  and the wall.

(7)

(Total 13 marks)



Q8.

A particle  $P$  of mass  $2m$  is moving in a straight line with speed  $3u$  on a smooth horizontal table. A second particle  $Q$  of mass  $3m$  is moving in the opposite direction to  $P$  along the same straight line with speed  $u$ . The particle  $P$  collides directly with  $Q$ . The direction of motion of  $P$  is reversed by the collision. The coefficient of restitution between  $P$  and  $Q$  is  $e$ .

(a) Show that the speed of  $Q$  immediately after the collision is  $\frac{u}{5}(8e + 3)$

(6)

(b) Find the range of possible values of  $e$ .

(4)

The total kinetic energy of the particles before the collision is  $T$ . The total kinetic energy of the particles after the collision is  $kT$ . Given that  $e = \frac{1}{2}$

(c) find the value of  $k$ .

(4)

(Total 14 marks)

(Q03 6678/01/R, June 2014)

Q9.

Two particles,  $A$  and  $B$ , are moving in opposite directions along the same straight line on a smooth horizontal surface when they collide directly.

Particle  $A$  has mass  $5m$  and particle  $B$  has mass  $3m$ .

The coefficient of restitution between  $A$  and  $B$  is  $e$ , where  $e > 0$

Immediately **after** the collision the speed of  $A$  is  $v$  and the speed of  $B$  is  $2v$ .

Given that  $A$  and  $B$  are moving in the same direction after the collision,

(a) find the set of possible values of  $e$ .

(8)

Given also that the kinetic energy of  $A$  immediately after the collision is 16% of the kinetic energy of  $A$  immediately before the collision,

(b) find

(i) the value of  $e$ ,

(ii) the magnitude of the impulse received by  $A$  in the collision, giving your answer in terms of  $m$  and  $v$ .

(6)

(Total for question = 14 marks)

(Q02 9FM0/03C, Oct 2021)